

--	--	--	--	--	--	--	--	--	--

G. VENKATASWAMY NAIDU COLLEGE (AUTONOMOUS), KOVILPATTI – 628 502.



UG DEGREE END SEMESTER EXAMINATIONS - APRIL 2025.

(For those admitted in June 2023 and later)

PROGRAMME AND BRANCH: B.Sc., MATHEMATICS

SEM	CATEGORY	COMPONENT	COURSE CODE	COURSE TITLE
IV	PART-III	CORE-8	U23MA408	ELEMENTS OF MATHEMATICAL ANALYSIS

Date & Session: 30.04.2025/AN

Time : 3 hours

Maximum: 75 Marks

Course Outcome	Bloom's K-level	Q. No.	SECTION – A (10 X 1 = 10 Marks) Answer ALL Questions.
CO1	K1	1.	What is the g.l.b of the sequence 1,2,3,4,..... a) 0 b) 1 c) 4 d) -1
CO1	K2	2.	Write the limit of the sequence $1/2^n$? a) 1 b) ∞ c) $1/2$ d) 0
CO2	K1	3.	Identify the limit of the sequence $\left(\frac{3n-4}{2n+7}\right)$ a) $3/2$ b) 0 c) $2/3$ d) $4/7$
CO2	K2	4.	If $ r < 1$, then $\lim_{n \rightarrow \infty} nr^n = \underline{\hspace{1cm}}$. a) n b) 1 c) ∞ d) 0
CO3	K1	5.	Which theorem states that $\lim_{n \rightarrow \infty} a_n^{\frac{1}{n}} = \lim_{n \rightarrow \infty} \frac{a_{n+1}}{a_n}$? a) Cauchy's Second limit theorem b) Cauchy's first limit theorem c) Cesaro's theorem d) Role's theorem
CO3	K2	6.	What will you say about the sequence 1, $1/2$, $1/3$, $1/4$, $1/n$, a) divergent b) convergent c) Oscillating d) monotonic
CO4	K1	7.	The geometric series $1+r+r^2+\dots+r^n+\dots$ converges to a) $\frac{r}{1-r}$ b) $\frac{1}{r-1}$ c) $\frac{1}{1+r}$ d) $\frac{1}{1-r}$
CO4	K2	8.	If $\sum a_n$ is a series of positive terms, then $\sum a_n$ converges if $\lim_{n \rightarrow \infty} \frac{a_n}{a_{n+1}} > 1$ and diverges if $\lim_{n \rightarrow \infty} \frac{a_n}{a_{n+1}} < 1$ this is which test? a) Comparison test b) Kummer's test c) D'Alembert's test d) Gauss's test
CO5	K1	9.	What is the nature of this series $\sum \frac{(-1)^n}{n}$? a) convergent b) conditionally convergent c) absolutely convergent d) divergent
CO5	K2	10.	Name the test which states that 'If $\sum a_n$ is a convergent series and (b_n) be a bounded monotonic sequence, then $\sum a_n b_n$ is convergent'. a) Leibnitz's test b) Dirichlet's test c) Abel's test d) Root test

Course Outcome	Bloom's K-level	Q. No.	SECTION – B (5 X 5 = 25 Marks) Answer ALL Questions choosing either (a) or (b)
CO1	K3	11a.	Prove that every convergent sequence is bounded. (OR)
CO1	K3	11b.	Prove that the sequence $((-1)^n)$ is not convergent.
CO2	K3	12a.	If $(a_n) \rightarrow 1, (b_n) \rightarrow 1$ and $a_n \leq c_n \leq b_n$ for all n , then prove that $(c_n) \rightarrow 1$. (OR)
CO2	K3	12b.	Show that $\lim_{n \rightarrow \infty} \frac{3n^2 + 2n + 5}{6n^2 + 4n + 7} = 1/2$.
CO3	K4	13a.	State and prove Cesaro's theorem. (OR)
CO3	K4	13b.	Prove that $\frac{1}{n} [n(n+1)(n+2) \dots n+n]^{1/n} \rightarrow 4/e$.
CO4	K4	14a.	Discuss the convergence of the series $\sum \frac{\sqrt{(n+1)} - \sqrt{n}}{n^p}$. (OR)
CO4	K4	14b.	Test the convergence of the series $1 + \frac{x^2}{2} + \frac{x^4}{4} + \frac{x^6}{6} + \dots$, where x is any positive real number.
CO5	K5	15a.	Show that the series $\sum (-1)^n [\sqrt{(n^2+1)} - n]$ is conditionally convergent (OR)
CO5	K5	15b.	If $\sum \frac{1}{n^2} = s$, then show that $1 + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{3}{4} s$

Course Outcome	Bloom's K-level	Q. No.	SECTION – C (5 X 8 = 40 Marks) Answer ALL Questions choosing either (a) or (b)
CO1	K3	16a.	i) Show that a sequence cannot converge to two different limits . ii) Prove that $\lim_{n \rightarrow \infty} \frac{1}{2^n} = 0$. (OR)
CO1	K3	16b.	i) Show that if (a_n) is a monotonic sequence then prove that $\left(\frac{a_1 + a_2 + \dots + a_n}{n}\right)$ is also a monotonic sequence. ii) Evaluate $\lim_{n \rightarrow \infty} \frac{n+1}{n}$.
CO2	K4	17a.	If $(a_n) \rightarrow a$ and $(b_n) \rightarrow b$, then prove that $(a_n + b_n) \rightarrow a + b$. (OR)
CO2	K4	17b.	Show that $\lim_{n \rightarrow \infty} \frac{\log n}{n^p} = 0$ if $p > 0$
CO3	K4	18a.	State and prove Cauchy's first limit theorem. (OR)
CO3	K4	18b.	Let (a_n) be a Cauchy sequence. If (a_n) has a subsequence (a_{n_k}) converges to l , then prove that $(a_n) \rightarrow l$.
CO4	K5	19a.	State and prove Comparison test. (OR)
CO4	K5	19b.	State and prove Cauchy's root test.
CO5	K5	20a.	Let $\sum (-1)^{n+1} a_n$ be an alternating series whose terms a_n satisfy following conditions (i) (a_n) is a monotonic decreasing sequence. (ii) $\lim_{n \rightarrow \infty} a_n = 0$. Then the given alternating series converges. Prove this statement. (OR)
CO5	K5	20b.	State and prove Abel's theorem.